

Larry Polansky (CCM/Music Dept.)  
Faculty Colloquia  
4/21/83  
Mills College

## Formal Theories of Musical Syntax

### I. Introduction to musical artificial intelligence and formal syntaxes.

#### A. Function of Modeling

1. Thom's kinematic and dynamic theories
2. Parametrization and prediction.

#### B. Role of theoretical constructs in music.

1. Revolutionary composition; Canetti's "decay of information and retardation of evolutionary progress".
2. Theoretical constructs as progressive steps-grounds for new composition.
3. Breakdown of conventional theoretical dogma.

#### C. Musical/historical role of theory

1. Often composers/theorists present musical and theoretical ideas simultaneously.

#### D. Development of a Formal Language

1. Simulation of natural languages.
2. Use of high speed intelligent devices.
3. Storage, decision making, and phenomenological stability of these devices.
4. Simulation of natural musical languages is in three categories: perception, composition, and performance.
5. Perceptual experiments.
6. Compositional experiments.
7. Performance experiments.

#### E. Statistical and morphological theories of musical language.

1. Language must integrate all three domains of musical activity.
2. Might be other classifications of theoretical investigation.

### II. Tenney's Perceptron-Design of a Statistical Formal Language

1. Proper design of musical parameters.
2. Gestalt segregation and cohesion.
3. Peak detection.
4. Hierarchical structuring.

Ex. 1

Ex. 2-7

5. Selected Examples
  - a. Sample input to program (from Varese).
  - b. First page of score of same with TG's.
  - c. First page of Ruggles' Portals.
  - d. 2 selected pages from FORTRAN program.
  - e. excerpt from Ruggles' paper showing comparison between perceptron and more conventional analysis.
  - f. map of intensity profiles-showing first hints of morphological considerations.

III. Morphological Theory

A. Practical usage.

1. Experimentation prior to complete statement of formal theory.
2. Rosenboom's On Being Invisible.
  - a) chart of performance system.
  - b) recording of performance (excerpts).

Example 8

M. Ex. 1

B. Morphological Metric spaces

1. Dynamic theory.
2. Shape.
3. Metric topology.
4. Metric= well-ordered space.
5. Sample metric (rough "curvature").
6. Other metrics.
7. Invariants.
8. Relationship to traditional musical terminology (esp. serialism).
9. Continuity--perception dependant.
10. L. Polansky Four Voice Canon #3 and #4
11. Page from Bemsha Swing (Polansky).
12. Nazca Liftoff (Rosenboom)

M. Ex. 2

Ex. 9

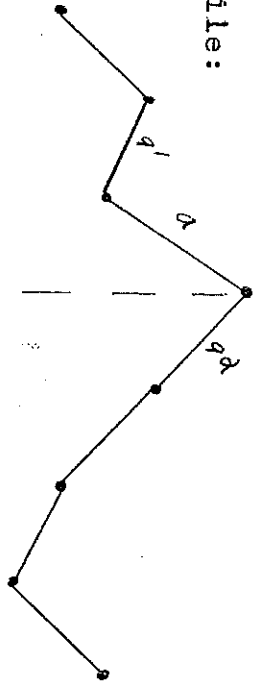
M. Ex. 3

## Selected References

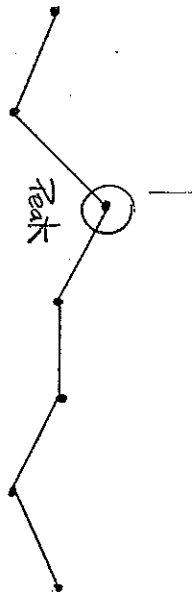
- Berlioz, H. Treatise on Instrumentation; trans. by Theodore Front;  
N.Y.; Kalmus, 1948  
(Good example of ostensibly theoretical treatise being more  
a statement of revolutionary compositional design).
- Greenberg, M.J. Euclidean and Non-Euclidean Geometries; S.F.; Freeman  
and Co.; 1973  
(Projectional geometry is essentially a study of morphological  
transformations--Greenberg's work is a good introduction to  
this powerful tool).
- Hiller, L., and Isaacson, L. "Illiatic Suite for String Quartet"; score;  
New Music; April; 1957  
(This piece is one of the pioneering examples of "stochastic"  
simulation of conventional form).
- Dugundji, James Topology; Allyn and Bacon; 1966.  
(The standard introduction and advanced text on point-set  
and beginning algebraic topology).
- Polansky, L. "A Hierarchical Gestalt Analysis of Ruggles' Portals";  
proceedings of 4th Int. Comp. Music Conference;  
1977; Northwestern U. Press.  
"Notes on the Proposed 68000 FORTH system music language"  
Internal CCM document, 1982.  
"Four Voice Canon #3 and Four Voice Canon #4"; 1975 and  
1979/82; available (rec.) on CCM Anthology Tape.
- Rothenberg, D. "A Model for Pattern Perception with Musical Applications"  
Part I-III; Jrnl. of Math. Systems Theory; #11 and  
12; 1978  
(Rothenberg's work is unique in its approach to the formalization  
of musical parameters and transformations. This is just one  
example of his voluminous output, much of it unpublished).
- Rosenboom, D. Biofeedback and the Arts; Toronto; ARC Pub.; 1976  
On Being Invisible (LP); ARC Recordings; 1977.  
Future Travel (LP); Street Records SRA-002; 1981  
"The Qualities of Change: "On Being Invisible": Steps  
Towards Transitional Topologies of Musical Form (1977:78: 82)"  
(unpublished ms.) 1982
- Tenney, J. (with Larry Polansky) "Hierarchical Temporal Gestalt Perception  
in Music: A 'Metric Space' Model"; Jrnl. of Music Theory; 1979.  
"META Meta/Hodos"; Jrnl. of Experimental Aesthetics; Vol 1 #1;  
Michael Byron, Ed.; Vancouver; ARC Pub.; 1978.
- Thom, R. Structural Stability and Morphogenesis; Trans. D.H. Fowler;  
W.A. Benjamin Inc.; 1975.
- Xenakis, Iannis Formalized Music; Indiana U. Press; 1971  
(Early statement by this groundbreaking composer on the possibilities  
of stochastic and algorithmic and probabilistic music).

EXAMPLE OF EVENT PROFILE AND CONSEQUENT  
DISJUNCTION MEASURE PROFILE.

Event profile:



Disjunction measure profile:



(disjunctions calculated as absolute values of corresponding events)

$$a > a'$$

$$a > a^2$$

# IX.B. Programme Output.

Input data: Varese

N	DUR	RST	PITCH	A.I	AZ	TMR
1	0-30	0-00	6-00	4-50	4-00	0-00
2	0-30	0-00	5-00	4-00	4-00	0-00
3	2-40	0-00	7-00	4-00	5-00	0-00
4	2-00	0-00	7-00	5-00	4-00	0-00
5	0-60	0-00	2-00	4-00	4-00	0-00
6	0-40	0-00	7-00	4-00	4-00	0-00
7	1-20	0-30	2-00	4-00	4-00	0-00
8	2-40	0-00	8-00	2-00	5-00	0-00
9	3-60	1-20	8-00	5-00	2-00	0-00
10	0-30	0-00	6-00	4-00	4-00	0-00
11	0-30	0-00	5-00	4-00	4-00	0-00
12	1-20	0-00	7-00	4-00	4-00	0-00
13	1-40	0-00	8-00	4-00	4-00	0-00
14	0-40	0-00	2-00	4-00	4-00	0-00
15	1-20	0-00	8-00	4-00	4-00	0-00
16	0-20	0-00	7-00	4-00	4-00	0-00
17	0-20	0-00	8-00	4-00	4-00	0-00
18	1-40	0-00	7-00	4-00	4-00	0-00
19	2-60	0-00	5-00	4-00	3-00	0-00
20	0-80	0-00	2-00	5-00	2-00	0-00
21	1-20	0-40	8-00	2-00	2-00	0-00
22	0-40	0-00	2-00	4-00	4-50	0-00
23	0-80	0-00	8-00	4-50	5-00	0-00
24	2-00	0-00	10-00	5-00	4-00	0-00
25	1-20	0-00	11-00	4-00	3-00	0-00
26	3-20	0-40	11-00	3-00	5-00	0-00
27	0-80	0-00	8-00	2-00	2-00	0-00
28	0-80	0-00	11-00	2-00	2-00	0-00
29	0-60	0-00	8-00	2-00	2-00	0-00
30	1-80	0-00	11-00	2-00	2-00	0-00
31	1-20	0-00	13-00	2-00	5-00	0-00
32	1-20	0-30	13-00	5-00	2-00	0-00
33	0-30	0-00	14-00	6-00	6-00	0-00
34	0-30	0-00	13-00	6-00	6-00	0-00
35	3-60	0-30	14-00	6-00	7-00	0-00
36	0-30	0-00	13-00	4-00	4-00	0-00
37	2-00	0-00	14-00	4-00	4-00	0-00
38	0-40	0-00	13-00	4-00	4-00	0-00
39	0-60	0-00	14-00	4-00	4-00	0-00
40	1-00	0-00	13-00	4-00	4-00	0-00
41	0-40	0-00	14-00	4-00	5-00	0-00
42	0-40	0-00	13-00	5-00	6-00	0-00
43	4-40	0-40	15-00	7-00	7-00	0-00
44	0-40	0-00	21-00	5-00	5-00	0-00
45	0-80	0-00	15-00	5-00	5-00	0-00
46	0-40	0-00	9-00	5-00	5-00	0-00
47	0-60	0-00	15-00	5-00	5-00	0-00
48	0-20	0-00	21-00	5-00	5-00	0-00
49	0-40	0-00	4-00	5-00	5-00	0-00
50	0-60	0-00	10-00	5-00	5-00	0-00
51	1-80	0-60	16-00	5-00	6-00	0-00
52	0-60	0-00	22-00	6-00	6-00	0-00
53	0-60	0-00	10-00	6-00	6-00	0-00
54	1-80	0-00	23-00	6-50	7-00	0-00
55	6-60	1-80	29-00	7-00	7-50	0-00
56	0-30	0-00	17-00	2-00	2-00	0-00
57	0-30	0-00	16-00	2-00	2-00	0-00
58	2-40	0-30	18-00	2-00	1-00	0-00

# IX.B. Programme Output.

Input data: Varese

N	DUR	RST	PITCH	A.I	A.Z	TMBR
1	0.30	0.00	6.00	4.50	4.00	0.00
2	0.30	0.00	5.00	4.00	4.00	0.00
3	2.40	0.00	7.00	4.00	5.00	0.00
4	2.00	0.00	7.00	5.00	4.00	0.00
5	0.60	0.00	2.00	4.00	4.00	0.00
6	0.40	0.00	7.00	4.00	4.00	0.00
7	1.20	0.30	2.00	4.00	4.00	0.00
8	2.40	0.00	8.00	2.00	5.00	0.00
9	3.60	1.20	8.00	5.00	2.00	0.00
10	0.30	0.00	6.00	4.00	4.00	0.00
11	0.30	0.00	5.00	4.00	4.00	0.00
12	1.20	0.00	7.00	4.00	4.00	0.00
13	1.40	0.00	8.00	4.00	4.00	0.00
14	0.40	0.00	2.00	4.00	4.00	0.00
15	1.20	0.00	8.00	4.00	4.00	0.00
16	0.20	0.00	7.00	4.00	4.00	0.00
17	0.20	0.00	8.00	4.00	4.00	0.00
18	1.40	0.00	7.00	4.00	4.00	0.00
19	2.60	0.00	5.00	4.00	3.00	0.00
20	0.80	0.00	2.00	5.00	2.00	0.00
21	1.20	0.40	8.00	2.00	2.00	0.00
22	0.40	0.00	2.00	4.00	4.50	0.00
23	0.80	0.00	8.00	4.50	5.00	0.00
24	2.00	0.00	10.00	5.00	4.00	0.00
25	1.20	0.00	11.00	4.00	3.00	0.00
26	3.20	0.40	11.00	3.00	5.00	0.00
27	0.80	0.00	8.00	2.00	2.00	0.00
28	0.80	0.00	11.00	2.00	2.00	0.00
29	0.60	0.00	8.00	2.00	2.00	0.00
30	1.80	0.00	11.00	2.00	2.00	0.00
31	1.20	0.00	13.00	2.00	5.00	0.00
32	1.20	0.30	13.00	5.00	2.00	0.00
33	0.30	0.00	14.00	6.00	6.00	0.00
34	0.30	0.00	13.00	6.00	6.00	0.00
35	3.60	0.30	14.00	6.00	7.00	0.00
36	0.30	0.00	13.00	4.00	4.00	0.00
37	2.00	0.00	14.00	4.00	4.00	0.00
38	0.40	0.00	13.00	4.00	4.00	0.00
39	0.60	0.00	14.00	4.00	4.00	0.00
40	1.00	0.00	13.00	4.00	4.00	0.00
41	0.40	0.00	14.00	4.00	5.00	0.00
42	0.40	0.00	13.00	5.00	6.00	0.00
43	4.40	0.40	15.00	7.00	7.00	0.00
44	0.40	0.00	21.00	5.00	5.00	0.00
45	0.80	0.00	15.00	5.00	5.00	0.00
46	0.40	0.00	9.00	5.00	5.00	0.00
47	0.60	0.00	15.00	5.00	5.00	0.00
48	0.20	0.00	21.00	5.00	5.00	0.00
49	0.40	0.00	4.00	5.00	5.00	0.00
50	0.60	0.00	10.00	5.00	5.00	0.00
51	1.80	0.60	16.00	5.00	6.00	0.00
52	0.60	0.00	22.00	6.00	6.00	0.00
53	0.60	0.00	10.00	6.00	6.00	0.00
54	1.80	0.00	23.00	6.50	7.00	0.00
55	6.60	1.80	29.00	7.00	7.50	0.00
56	0.30	0.00	17.00	2.00	2.00	0.00
57	0.30	0.00	16.00	2.00	2.00	0.00
58	2.40	0.30	18.00	2.00	1.00	0.00

Saxophone I  
Saxophone II  
Saxophone III  
Clarinet

$\text{♩} = 72^{**}$

Hierarchical structure from Nattiez (1975)

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Figure IV.1. Edgard Varèse: DENSITY 21.5 --- final results with "optimum" weightings (above), and segmentation according to Nattiez (below).

Section 1

Ruggles; Portals; (melodic line)

Segment 1

Optimal weights: Proximity = 1; Pitch (PW) = .5; Intensity (IW) = 2

Temporal Density = 1; Timbre = .2

21

Segment 1

2

Clang 1

2

3

4

5

6

1 Moderato

Variant weightings: PW = .3 (all other parameters as above)

PW = .6 (all other parameters as above)

IW = 3 (all other parameters as above)

MP



```

2 F5.2, ' TIMBRE=', F5.2)
50 WSUM=PW+DW+TDW+AW+TW
51 PW=PW/WSUM
52 DW=DW/WSUM
53 TDW=TDW/WSUM
54 AW=AW/WSUM
55 TW=TW/WSUM
56 DO 76 K=1,10
57 76 COUNT(K)=0
58 DO 78 K=1,1000
59 DM(K)=0.0
60 DMST(K)=0.
61 DMD1(K)=0
62 DMD2(K)=0
63 IEND(K)=0
64 78 ISTART(K)=0
C
65 DA=DW*10.0
C
C INITIALIZES BOUNDARIES ON FIRST LEVEL
66 DO 1777 I=2,N
67 PI=PW*(P1(I)-P2(I-1))
68 TDI=0.0
69 DI=DW*(RST(I-1))
70 IF (RST(I-1).EQ.0.)ALAST=A2(I-1)
71 IF(RST(I-1).GT.0.)ALAST=0.
72 AI=AW*(A1(I)-ALAST)
73 DM(I)=(ABS(DI)+ABS(PI)+ABS(TDI)+ABS(AI))
74 DM(I)=DM(I)*2.0
C
75 1777 CONTINUE
76 DO 80 I=501,1000
77 P(I)=0
78 DUR(I)=0
79 AMP(I)=0
80 TD(I)=0
81 TIM(I)=0
82 RST(I)=0
83 80 CONTINUE
C
84 LEVEL=0
C
C MAIN PROGRAM
C
C SETS NEW LEVEL, CLEARS COUNTER(CHECK), AND INITIALIZES
C FLAG, WHICH TELLS YOU IF YOU'VE FINISHED ON A LEVEL.
C CHECK IS A VARIABLE WHICH SEES IF THERE ARE ENOUGH
C TG'S CURRENTLY TO COMPUTE FOR INITIATION.
C
85 100 CHECK=0
86 ET=0.
87 FLAG=0
88 LEVEL=LEVEL+1
C
C SETS ARRAY INDICES.
89 LOLEV= (2.0**(LEVEL-1))
90 HILEV= (2.0**(LEVEL))

```

```

91      K1=1000.0-((1.0/LOLEV)*1000.0)
92      K2=1000.0-((1.0/HILEV)*1000.0)
93      WRITE(6,9375)
      C
      C      IF NUMBER<4, THEN NOT ENOUGH TG'S ON THIS HIGHEST LEVEL
      C      TO TRY AND MAKE DISTINCTIONS. SO PROGRAM TERMINATES.
94      IF (NUMBER(LEVEL).LT.4) GO TO 9000
95      HICNT=I
96      ISTART(K2+1)=K1+1
      C
      C      SPECIFIC PLANAR COMPUTATION
97      500      COUNT(LEVEL)=COUNT(LEVEL)+1
98      TCOUNT=COUNT(LEVEL)
99      CHECK=CHECK+1
100     IF (TCOUNT.LE.NUMBER(LEVEL)) GO TO 550
101     FLAG=1
102     GO TO 700
      C
      C
      C      KEEPS TRACK OF ELAPSED TIME IN TG.
103     550     ET=ET+DUR(TCOUNT+K1)
      C
      C      CHECKS FOR 'ONE ELEMENT CLANGS'.
104     IF (CHECK.LT.2) GO TO 500
      C
      C      COMPUTE INTERVAL (DISJUNCTION MEASURE)
105     IND=(TCOUNT+K1)
      C
      C      MEAN INTERVALS
106     PI=PW*(P(IND)-P(IND-1))
107     DI=DW*DUR(IND-1)
108     IF (LEVEL.GT.1) DI=0.
109     TDI=TDW*(TD(IND)-TD(IND-1))
110     AI=AW*(AMP(IND)-AMP(IND-1))
111     TI=TW*(TIM(IND)-TIM(IND-1))
      C      SUMS MEAN INTERVALS.
112     ABSUM=ABS(PI)+ABS(TDI)+ABS(AI)+ABS(TI)+DI
      C
      C
      C      "CITY-BLOCK" METRIC.
113     DM(IND)=.5*DM(IND)+ABSUM
      C
114     IF (TCOUNT.LT.4) GO TO 650
      C
      C      COMPUTES DIFFERENCE OF PEAK WITH SURROUNDING DM'S TO GIVE
      C      ROUGH IDEA OF STRENGTH OF INITIATOR.
115     DMD1(IND-1)=1.0-(DM(IND-2)/DM(IND-1))
116     DMD2(IND-1)=1.0-(DM(IND)/DM(IND-1))
      C
117     650     IF (CHECK.LT.4) GO TO 500
      C
      C      CHECKS MINIMUM TG LENGTH.
118     ETCHK=ET-(DUR(IND-1)+DUR(IND))
119     IF (ETCHK.LE.CMIN) GO TO 500
      C
      C      TESTS FOR PEAK.
120     IF ((DMD1(IND-1).LT.EPS1).OR.(DMD2(IND-1).LT.EPS1))
1      GO TO 500
      C
      C      IF DMST POSITIVE, THEN PEAK. IF ZERO, THEN NOT PEAK.

```

GENERAL COMMENTS

The larger hierarchical segmentation resulting from the optimal weights is as follows:

		<u>EL. #</u>	<u>MEASURES</u>
SECTION I	SEGMENT 1	1-24	1-6
	SEGMENT 2	25-46	6-9
	SEGMENT 3	46-57	10-13
SECTION II	SEGMENT 4	58-89	13-19
	SEGMENT 5	90-128	19-25
SECTION III	SEGMENT 6	129-188	26-35
	SEGMENT 7	189-207	36-38
	SEGMENT 8	208-249	39-46
	SEGMENT 9	250-261	47-50
SECTION IV	SEGMENT 10	262-292	50-54
	SEGMENT 11	293-320	54-59
	SEGMENT 12	321-379	59-69
	SEGMENT 13	380-408	70-75

Thomas Peterson, in The Music of Carl Ruggles, states that Portals has "... a certain semblance to rondo form, since the principle idea recurs (albeit in freely varied fashion) four times during the course of the work, as well as providing the material for the coda. A plausible attempt at conventional analysis might be made as follows:

A	1-6	B	43-50
B	6-13	D	50-62
A <sup>1</sup>	13-19	A <sup>3</sup>	62-70
C	19-26	CODA	70-75 (based on A)" <sup>1</sup>
A <sup>2</sup>	26-43		

# Inversion Profile (all levels) (Section III)

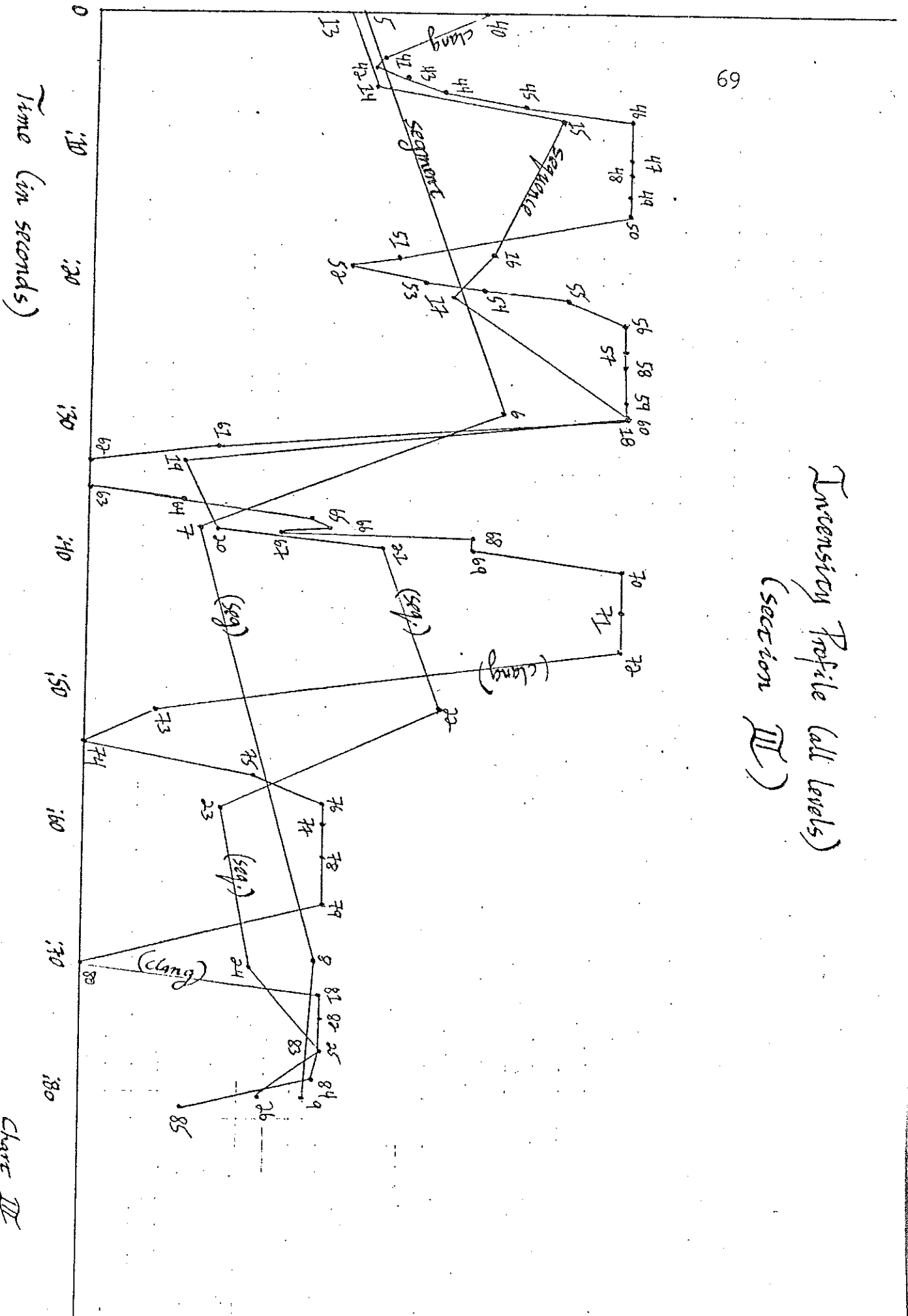


Chart III

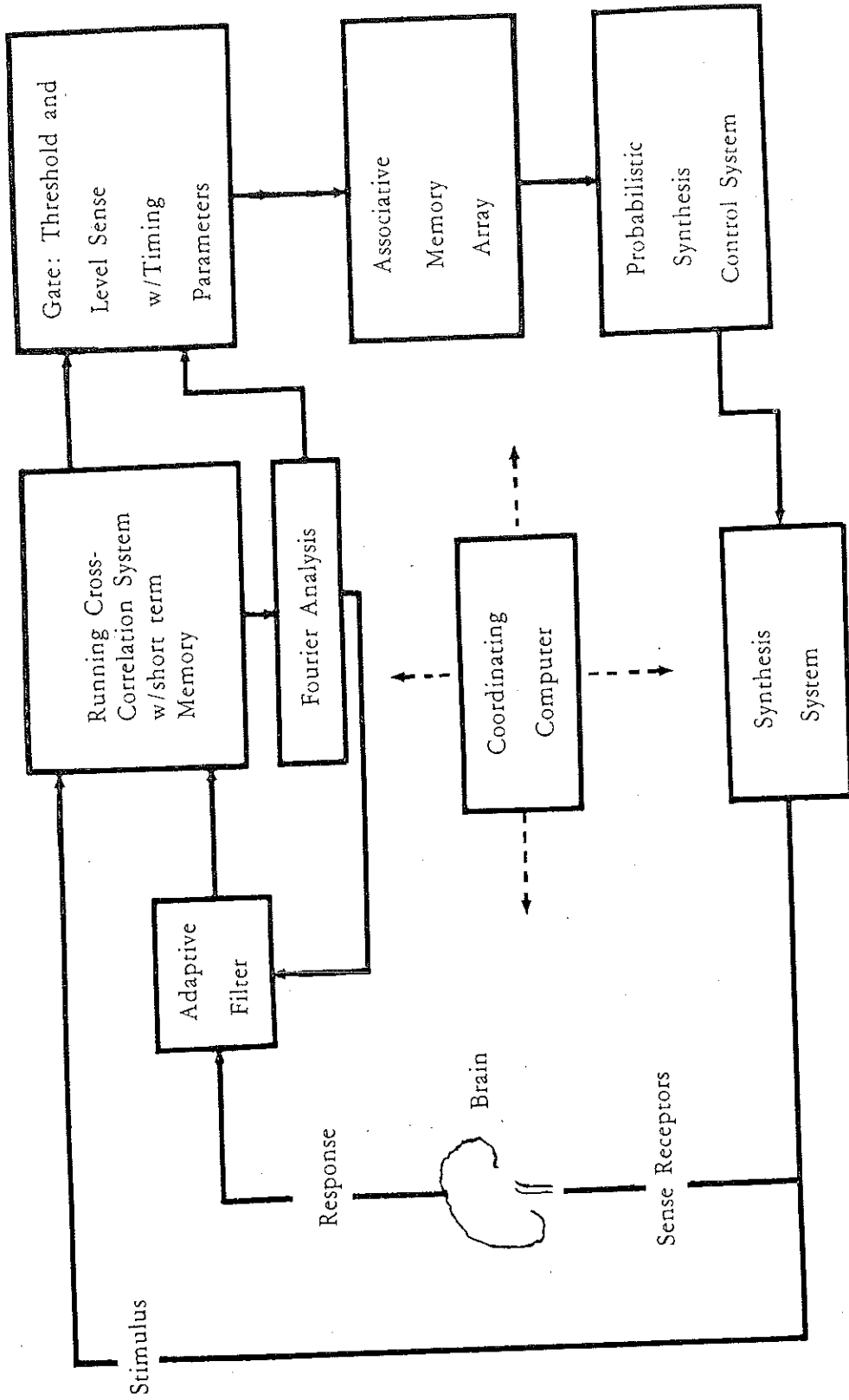


Figure 2.

The first system consists of two staves. The top staff is a guitar staff with a treble clef, showing a sequence of chords and melodic lines with fingerings 3, 3, 3, 3, 3, 5, 3, 3, 3, 5, 3, 6. The bottom staff is a piano staff with a treble clef, showing a corresponding melodic line with fingerings 3, 3, 3, 3, 5, 3, 3, 5, 3, 6, 7. A circled asterisk (\*) is placed above the piano staff.

The second system continues the piece with similar notation. The guitar staff has fingerings 3, 3, 3, 3, 3, 5, 3, 3, 3, 6. The piano staff has fingerings 3, 3, 3, 3, 5, 3, 5, 6, 7. A circled asterisk (\*) is placed above the piano staff.

The third system continues the piece. The guitar staff has fingerings 3, 3, 3, 3, 3, 5, 3, 3, 3, 6. The piano staff has fingerings 3, 3, 3, 3, 5, 3, 5, 6, 7. A circled asterisk (\*) is placed above the piano staff.

The fourth system continues the piece. The guitar staff has fingerings 3, 3, 3, 3, 3, 5, 3, 3, 3, 6. The piano staff has fingerings 3, 3, 3, 3, 5, 3, 5, 6, 7. A circled asterisk (\*) is placed above the piano staff.

The fifth system continues the piece. The guitar staff has fingerings 3, 3, 3, 3, 3, 5, 3, 3, 3, 6. The piano staff has fingerings 3, 3, 3, 3, 5, 3, 5, 6, 7. A circled asterisk (\*) is placed above the piano staff.

The sixth system continues the piece. The guitar staff has fingerings 3, 3, 3, 3, 3, 5, 3, 3, 3, 6. The piano staff has fingerings 3, 3, 3, 3, 5, 3, 5, 6, 7. A circled asterisk (\*) is placed above the piano staff.

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The seventh system continues the piece. The guitar staff has fingerings 3, 3, 3, 3, 3, 5, 3, 3, 3, 6. The piano staff has fingerings 3, 3, 3, 3, 5, 3, 5, 6, 7. A circled asterisk (\*) is placed above the piano staff.